

## 4,4'-(Cyclohexane-1,1-diyl)dianilinium dichloride monohydrate

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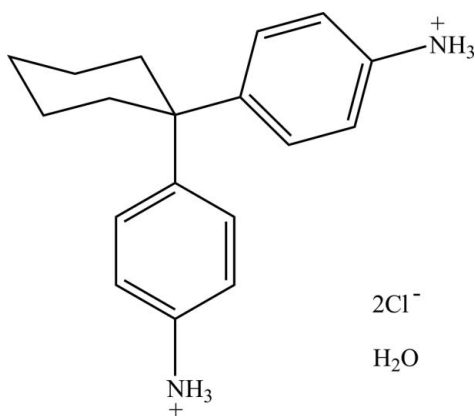
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Key indicators: single-crystal X-ray study;  $T = 291$  K; mean  $\sigma(\text{C}-\text{C}) = 0.005$  Å;  $R$  factor = 0.065;  $wR$  factor = 0.212; data-to-parameter ratio = 13.8.

In the title compound,  $\text{C}_{18}\text{H}_{24}\text{N}_2^{2+} \cdot 2\text{Cl}^- \cdot \text{H}_2\text{O}$ , both the cation and the water molecule lie on a twofold crystallographic axis. In the cation, the two benzene rings are perpendicular to each other, making a symmetry-constrained dihedral angle of  $90^\circ$ . In the crystal,  $\text{N}-\text{H} \cdots \text{Cl}$ ,  $\text{O}-\text{H} \cdots \text{Cl}$  and  $\text{N}-\text{H} \cdots \text{O}$  hydrogen bonds result in the formation of a three-dimensional network.

### Related literature

For related structures, see: Hanton *et al.* (1992); Qian & Huang (2010).



### Experimental

#### Crystal data

 $\text{C}_{18}\text{H}_{24}\text{N}_2^{2+} \cdot 2\text{Cl}^- \cdot \text{H}_2\text{O}$ 
 $M_r = 357.31$ 

Monoclinic,  $P2_1/m$   
 $a = 8.442$  (3) Å  
 $b = 9.548$  (4) Å  
 $c = 12.098$  (5) Å  
 $\beta = 107.085$  (5)°  
 $V = 932.1$  (6) Å<sup>3</sup>

$Z = 2$   
 Mo  $K\alpha$  radiation  
 $\mu = 0.35$  mm<sup>-1</sup>  
 $T = 291$  K  
 $0.12 \times 0.12 \times 0.10$  mm

#### Data collection

Bruker 1K CCD area-detector diffractometer  
 Absorption correction: multi-scan (SADABS; Bruker, 2000)  
 $T_{\min} = 0.959$ ,  $T_{\max} = 0.965$

4705 measured reflections  
 1735 independent reflections  
 1158 reflections with  $I > 2\sigma(I)$   
 $R_{\text{int}} = 0.102$

#### Refinement

$R[F^2 > 2\sigma(F^2)] = 0.065$   
 $wR(F^2) = 0.212$   
 $S = 1.10$   
 1735 reflections

126 parameters  
 H-atom parameters constrained  
 $\Delta\rho_{\text{max}} = 0.74$  e Å<sup>-3</sup>  
 $\Delta\rho_{\text{min}} = -0.51$  e Å<sup>-3</sup>

**Table 1**

Hydrogen-bond geometry (Å, °).

$D-H \cdots A$	$D-H$	$H \cdots A$	$D \cdots A$	$D-H \cdots A$
$\text{N2}-\text{H2C} \cdots \text{Cl1}^{\text{i}}$	0.89	2.70	3.253 (3)	121
$\text{N2}-\text{H2C} \cdots \text{Cl1}^{\text{ii}}$	0.89	2.53	3.252 (3)	139
$\text{N2}-\text{H2B} \cdots \text{Cl1}^{\text{iii}}$	0.89	2.41	3.253 (3)	159
$\text{N2}-\text{H2A} \cdots \text{Cl1}^{\text{iv}}$	0.89	2.46	3.252 (3)	148
$\text{O1}-\text{H1E} \cdots \text{Cl1}^{\text{v}}$	0.85	2.42	3.183 (3)	150
$\text{O1}-\text{H1D} \cdots \text{Cl1}^{\text{vi}}$	0.82	2.38	3.183 (3)	167
$\text{N1}-\text{H1C} \cdots \text{Cl1}^{\text{vii}}$	0.90	2.22	3.101 (3)	165
$\text{N1}-\text{H1B} \cdots \text{O1}^{\text{viii}}$	0.90	1.78	2.678 (6)	172
$\text{N1}-\text{H1A} \cdots \text{Cl1}^{\text{ix}}$	0.90	2.23	3.101 (3)	163

Symmetry codes: (i)  $x + 1, -y + \frac{3}{2}, z$ ; (ii)  $-x + 2, y - \frac{1}{2}, -z + 1$ ; (iii)  $x + 1, y - 1, z$ ; (iv)  $-x + 2, -y + 1, -z + 1$ ; (v)  $-x + 1, -y + 1, -z + 1$ ; (vi)  $-x + 1, y - \frac{1}{2}, -z + 1$ ; (vii)  $x + 1, y - 1, z - 1$ ; (viii)  $x, y, z - 1$ ; (ix)  $x + 1, -y + \frac{3}{2}, z - 1$ .

Data collection: *SMART* (Bruker, 2000); cell refinement: *SAINTE* (Bruker, 2000); data reduction: *SAINTE*; program(s) used to solve structure: *SHELXTL* (Sheldrick, 2008); program(s) used to refine structure: *SHELXTL*; molecular graphics: *SHELXTL*; software used to prepare material for publication: *SHELXTL*.

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: FF2022).

### References

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 Sheldrick, G. M. (2008). *Acta Cryst.* **A64**, 112–122.

**supplementary materials**

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## 4,4'-(Cyclohexane-1,1-diyl)dianilinium dichloride monohydrate

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### Comment

There have been only one related single-crystal structural report on 1,1-bis(4-amino-3,5-dimethylphenyl)cyclohexane (Hanton *et al.*, 1992). We have previously reported the single-crystal structure of a similar compound biphenyl-3,3',4,4'-tetraamine (Qian & Huang, 2010). In this work, we describe the single-crystal structure of hydrochloride salt of 1,1-bis(4-aminophenyl)cyclohexane.

The atom-numbering scheme of the title compound is shown in Fig. 1, while selected bond distances and bond angles are given in Table 1. The two phenyl rings of the title compound are perpendicular to each other with a dihedral angle of 90°. In the crystal packing, N—H...Cl and O—H...Cl hydrogen-bond interactions give rise to a three-dimensional network.

### Experimental

The treatment of 1,1-bis(4-aminophenyl)cyclohexane dissolved in methanol with an excess of hydrochloric acid yields the title compound. Single crystals suitable for X-ray diffraction measurement were obtained after 7 days' slow evaporation of the mother liquid at room temperature in air. Anal. Calcd. For C<sub>18</sub>H<sub>24</sub>N<sub>2</sub><sup>2+</sup>·2Cl<sup>-</sup>·H<sub>2</sub>O: C, 60.50; H, 7.33; N, 7.84%. Found: C, 60.31; H, 7.55; N, 7.96%.

### Refinement

The non-hydrogen atoms were refined anisotropically, whereas the H atoms bonded with carbon, nitrogen and oxygen atoms were placed in geometrically idealized positions (C—H = 0.93 or 0.97 Å, N—H = 0.89 Å and O—H = 0.82 or 0.85 Å) and refined as riding atoms, with  $U_{\text{iso}}(\text{H}) = 1.2U_{\text{eq}}(\text{C})$  and  $1.2U_{\text{eq}}(\text{N})$  and  $U_{\text{iso}}(\text{H}) = 1.5U_{\text{eq}}(\text{O})$ . The hydrogen atoms bonded to atoms O1 and N2 are refined as the model with split positions.

### Figures

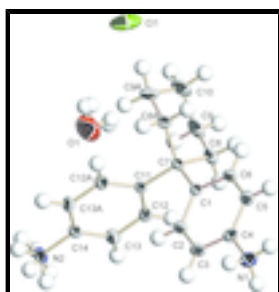


Fig. 1. An ORTEP drawing of the title compound with the atom-numbering scheme. Displacement ellipsoids are drawn at the 30% probability level. [Symmetry codes: (A)  $x, 0.5-y, z$ ]

## 4,4'-(Cyclohexane-1,1-diyl)dianilinium dichloride monohydrate

### Crystal data

$C_{18}H_{24}N_2^{2+} \cdot 2Cl^- \cdot H_2O$	$F(000) = 380$
$M_r = 357.31$	$D_x = 1.273 \text{ Mg m}^{-3}$
Monoclinic, $P2_1/m$	Mo $K\alpha$ radiation, $\lambda = 0.71073 \text{ \AA}$
Hall symbol: $-P\ 2yb$	Cell parameters from 1254 reflections
$a = 8.442(3) \text{ \AA}$	$\theta = 2.5\text{--}24.5^\circ$
$b = 9.548(4) \text{ \AA}$	$\mu = 0.35 \text{ mm}^{-1}$
$c = 12.098(5) \text{ \AA}$	$T = 291 \text{ K}$
$\beta = 107.085(5)^\circ$	Block, colourless
$V = 932.1(6) \text{ \AA}^3$	$0.12 \times 0.12 \times 0.10 \text{ mm}$
$Z = 2$	

### Data collection

Bruker 1K CCD area-detector diffractometer	1735 independent reflections
Radiation source: fine-focus sealed tube graphite	1158 reflections with $I > 2\sigma(I)$
$\varphi$ and $\omega$ scans	$R_{\text{int}} = 0.102$
Absorption correction: multi-scan (SADABS; Bruker, 2000)	$\theta_{\text{max}} = 25.0^\circ$ , $\theta_{\text{min}} = 1.8^\circ$
$T_{\text{min}} = 0.959$ , $T_{\text{max}} = 0.965$	$h = -8 \rightarrow 10$
4705 measured reflections	$k = -11 \rightarrow 10$
	$l = -14 \rightarrow 13$

### Refinement

Refinement on $F^2$	Primary atom site location: structure-invariant direct methods
Least-squares matrix: full	Secondary atom site location: difference Fourier map
$R[F^2 > 2\sigma(F^2)] = 0.065$	Hydrogen site location: inferred from neighbouring sites
$wR(F^2) = 0.212$	H-atom parameters constrained
$S = 1.10$	$w = 1/[\sigma^2(F_o^2) + (0.1167P)^2]$
1735 reflections	where $P = (F_o^2 + 2F_c^2)/3$
126 parameters	$(\Delta/\sigma)_{\text{max}} < 0.001$
0 restraints	$\Delta\rho_{\text{max}} = 0.74 \text{ e \AA}^{-3}$
	$\Delta\rho_{\text{min}} = -0.51 \text{ e \AA}^{-3}$

### Special details

**Experimental.** The structure was solved by direct methods (Bruker, 2000) and successive difference Fourier syntheses.

**Geometry.** All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations

between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

**Refinement.** Refinement of  $F^2$  against ALL reflections. The weighted  $R$ -factor  $wR$  and goodness of fit  $S$  are based on  $F^2$ , conventional  $R$ -factors  $R$  are based on  $F$ , with  $F$  set to zero for negative  $F^2$ . The threshold expression of  $F^2 > \sigma(F^2)$  is used only for calculating  $R$ -factors(gt) *etc.* and is not relevant to the choice of reflections for refinement.  $R$ -factors based on  $F^2$  are statistically about twice as large as those based on  $F$ , and  $R$ -factors based on ALL data will be even larger.

*Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters ( $\text{\AA}^2$ )*

	<i>x</i>	<i>y</i>	<i>z</i>	$U_{\text{iso}}^*/U_{\text{eq}}$	Occ. (<1)
C1	0.9232 (4)	0.2500	-0.0868 (3)	0.0294 (9)	
C2	1.0908 (5)	0.2500	-0.0779 (3)	0.0359 (9)	
H2	1.1675	0.2500	-0.0048	0.043*	
C3	1.1484 (5)	0.2500	-0.1747 (4)	0.0417 (10)	
H3	1.2616	0.2500	-0.1659	0.050*	
C4	1.0383 (5)	0.2500	-0.2816 (3)	0.0386 (10)	
C5	0.8702 (5)	0.2500	-0.2956 (3)	0.0425 (10)	
H5	0.7954	0.2500	-0.3694	0.051*	
C6	0.8136 (5)	0.2500	-0.1994 (3)	0.0372 (10)	
H6	0.7000	0.2500	-0.2095	0.045*	
C7	0.8564 (4)	0.2500	0.0183 (3)	0.0319 (9)	
C8	0.7457 (3)	0.1189 (3)	0.0130 (2)	0.0424 (8)	
H8A	0.6611	0.1165	-0.0613	0.051*	
H8B	0.8131	0.0354	0.0190	0.051*	
C9	0.6634 (4)	0.1176 (4)	0.1081 (3)	0.0613 (11)	
H9A	0.7474	0.1105	0.1824	0.074*	
H9B	0.5920	0.0362	0.0991	0.074*	
C10	0.5613 (6)	0.2500	0.1054 (4)	0.077 (2)	
H10A	0.4679	0.2500	0.0358	0.092*	
H10B	0.5181	0.2500	0.1713	0.092*	
C11	1.0029 (4)	0.2500	0.1307 (3)	0.0305 (9)	
C12	1.0744 (3)	0.1265 (3)	0.1817 (2)	0.0403 (8)	
H12	1.0283	0.0417	0.1503	0.048*	
C13	1.2123 (4)	0.1256 (3)	0.2777 (2)	0.0436 (8)	
H13	1.2590	0.0414	0.3101	0.052*	
C14	1.2789 (5)	0.2500	0.3243 (3)	0.0362 (10)	
Cl1	0.35794 (16)	1.02159 (14)	0.60558 (11)	0.1036 (6)	
N1	1.1019 (5)	0.2500	-0.3833 (3)	0.0507 (10)	
H1A	1.1617	0.3283	-0.3818	0.061*	0.50
H1B	1.0163	0.2500	-0.4484	0.061*	
H1C	1.1641	0.1729	-0.3814	0.061*	0.50
N2	1.4267 (4)	0.2500	0.4255 (3)	0.0493 (10)	
H2A	1.5082	0.2037	0.4086	0.059*	0.50
H2B	1.4031	0.2084	0.4846	0.059*	0.50
H2C	1.4584	0.3378	0.4446	0.059*	0.50
O1	0.8669 (6)	0.2500	0.4122 (4)	0.128 (2)	
H1D	0.8043	0.3178	0.3960	0.192*	0.50
H1E	0.7860	0.1950	0.3841	0.192*	0.50

## supplementary materials

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### Atomic displacement parameters ( $\text{\AA}^2$ )

	$U^{11}$	$U^{22}$	$U^{33}$	$U^{12}$	$U^{13}$	$U^{23}$
C1	0.030 (2)	0.025 (2)	0.032 (2)	0.000	0.0082 (15)	0.000
C2	0.030 (2)	0.039 (2)	0.039 (2)	0.000	0.0105 (16)	0.000
C3	0.035 (2)	0.046 (3)	0.048 (2)	0.000	0.0184 (19)	0.000
C4	0.041 (2)	0.041 (2)	0.041 (2)	0.000	0.0226 (19)	0.000
C5	0.044 (2)	0.046 (3)	0.036 (2)	0.000	0.0099 (18)	0.000
C6	0.028 (2)	0.043 (2)	0.041 (2)	0.000	0.0109 (17)	0.000
C7	0.0252 (19)	0.036 (2)	0.033 (2)	0.000	0.0060 (15)	0.000
C8	0.0352 (16)	0.054 (2)	0.0357 (15)	-0.0139 (14)	0.0078 (12)	0.0014 (13)
C9	0.0405 (18)	0.099 (3)	0.0450 (18)	-0.0282 (19)	0.0127 (14)	0.0056 (18)
C10	0.035 (3)	0.155 (6)	0.045 (3)	0.000	0.018 (2)	0.000
C11	0.0286 (19)	0.035 (2)	0.0291 (19)	0.000	0.0101 (15)	0.000
C12	0.0418 (17)	0.0318 (16)	0.0425 (16)	0.0008 (13)	0.0051 (13)	-0.0019 (12)
C13	0.0439 (17)	0.0334 (17)	0.0456 (17)	0.0044 (13)	0.0007 (13)	0.0073 (13)
C14	0.030 (2)	0.043 (2)	0.033 (2)	0.000	0.0056 (17)	0.000
C11	0.1165 (11)	0.1117 (11)	0.1092 (10)	0.0666 (8)	0.0747 (8)	0.0572 (7)
N1	0.053 (2)	0.057 (3)	0.050 (2)	0.000	0.0262 (18)	0.000
N2	0.041 (2)	0.058 (3)	0.039 (2)	0.000	-0.0023 (15)	0.000
O1	0.106 (4)	0.199 (7)	0.067 (3)	0.000	0.007 (3)	0.000

### Geometric parameters ( $\text{\AA}$ , $^\circ$ )

C1—C2	1.388 (5)	C9—H9B	0.9700
C1—C6	1.404 (5)	C10—C9 <sup>i</sup>	1.525 (5)
C1—C7	1.535 (5)	C10—H10A	0.9700
C2—C3	1.393 (5)	C10—H10B	0.9700
C2—H2	0.9300	C11—C12 <sup>i</sup>	1.384 (3)
C3—C4	1.352 (6)	C11—C12	1.384 (3)
C3—H3	0.9300	C12—C13	1.383 (4)
C4—C5	1.379 (6)	C12—H12	0.9300
C4—N1	1.480 (5)	C13—C14	1.363 (3)
C5—C6	1.382 (5)	C13—H13	0.9300
C5—H5	0.9300	C14—C13 <sup>i</sup>	1.363 (3)
C6—H6	0.9300	C14—N2	1.469 (5)
C7—C11	1.546 (5)	N1—H1A	0.8993
C7—C8	1.552 (4)	N1—H1B	0.8990
C7—C8 <sup>i</sup>	1.552 (4)	N1—H1C	0.9005
C8—C9	1.508 (4)	N2—H2A	0.8900
C8—H8A	0.9700	N2—H2B	0.8900
C8—H8B	0.9700	N2—H2C	0.8900
C9—C10	1.525 (5)	O1—H1D	0.8217
C9—H9A	0.9700	O1—H1E	0.8491
C2—C1—C6	116.2 (3)	C10—C9—H9B	109.4
C2—C1—C7	123.4 (3)	H9A—C9—H9B	108.0
C6—C1—C7	120.4 (3)	C9 <sup>i</sup> —C10—C9	112.0 (4)

C1—C2—C3	122.3 (4)	C9 <sup>i</sup> —C10—H10A	109.2
C1—C2—H2	118.9	C9—C10—H10A	109.2
C3—C2—H2	118.9	C9 <sup>i</sup> —C10—H10B	109.2
C4—C3—C2	119.5 (4)	C9—C10—H10B	109.2
C4—C3—H3	120.3	H10A—C10—H10B	107.9
C2—C3—H3	120.3	C12 <sup>i</sup> —C11—C12	116.8 (3)
C3—C4—C5	120.7 (4)	C12 <sup>i</sup> —C11—C7	121.54 (17)
C3—C4—N1	118.7 (3)	C12—C11—C7	121.54 (17)
C5—C4—N1	120.6 (4)	C13—C12—C11	121.9 (3)
C4—C5—C6	119.7 (4)	C13—C12—H12	119.0
C4—C5—H5	120.2	C11—C12—H12	119.0
C6—C5—H5	120.2	C14—C13—C12	119.0 (3)
C5—C6—C1	121.6 (4)	C14—C13—H13	120.5
C5—C6—H6	119.2	C12—C13—H13	120.5
C1—C6—H6	119.2	C13—C14—C13 <sup>i</sup>	121.2 (3)
C1—C7—C11	109.6 (3)	C13—C14—N2	119.38 (18)
C1—C7—C8	109.2 (2)	C13 <sup>i</sup> —C14—N2	119.38 (18)
C11—C7—C8	110.63 (19)	C4—N1—H1A	108.8
C1—C7—C8 <sup>i</sup>	109.2 (2)	C4—N1—H1B	109.5
C11—C7—C8 <sup>i</sup>	110.63 (19)	H1A—N1—H1B	108.6
C8—C7—C8 <sup>i</sup>	107.5 (3)	C4—N1—H1C	109.3
C9—C8—C7	112.4 (3)	H1A—N1—H1C	111.0
C9—C8—H8A	109.1	H1B—N1—H1C	109.6
C7—C8—H8A	109.1	C14—N2—H2A	109.5
C9—C8—H8B	109.1	C14—N2—H2B	109.5
C7—C8—H8B	109.1	H2A—N2—H2B	109.5
H8A—C8—H8B	107.8	C14—N2—H2C	109.5
C8—C9—C10	111.2 (3)	H2A—N2—H2C	109.5
C8—C9—H9A	109.4	H2B—N2—H2C	109.5
C10—C9—H9A	109.4	H1D—O1—H1E	90.4
C8—C9—H9B	109.4		
C6—C1—C2—C3	0.0	C1—C7—C8—C9	-175.1 (2)
C7—C1—C2—C3	180.0	C11—C7—C8—C9	64.2 (3)
C1—C2—C3—C4	0.0	C8 <sup>i</sup> —C7—C8—C9	-56.7 (4)
C2—C3—C4—C5	0.0	C7—C8—C9—C10	56.5 (3)
C2—C3—C4—N1	180.0	C8—C9—C10—C9 <sup>i</sup>	-53.9 (5)
C3—C4—C5—C6	0.0	C1—C7—C11—C12 <sup>i</sup>	88.2 (3)
N1—C4—C5—C6	180.0	C8—C7—C11—C12 <sup>i</sup>	-151.3 (3)
C4—C5—C6—C1	0.0	C8 <sup>i</sup> —C7—C11—C12 <sup>i</sup>	-32.3 (4)
C2—C1—C6—C5	0.0	C1—C7—C11—C12	-88.2 (3)
C7—C1—C6—C5	180.0	C8—C7—C11—C12	32.3 (4)
C2—C1—C7—C11	0.0	C8 <sup>i</sup> —C7—C11—C12	151.3 (3)
C6—C1—C7—C11	180.0	C12 <sup>i</sup> —C11—C12—C13	-1.0 (5)
C2—C1—C7—C8	-121.3 (2)	C7—C11—C12—C13	175.6 (3)
C6—C1—C7—C8	58.7 (2)	C11—C12—C13—C14	0.6 (5)

## supplementary materials

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C2—C1—C7—C8 <sup>i</sup>	121.3 (2)	C12—C13—C14—C13 <sup>i</sup>	-0.2 (6)
C6—C1—C7—C8 <sup>i</sup>	-58.7 (2)	C12—C13—C14—N2	-179.2 (3)

Symmetry codes: (i)  $x, -y+1/2, z$ .

### Hydrogen-bond geometry (Å, °)

<i>D</i> —H... <i>A</i>	<i>D</i> —H	H... <i>A</i>	<i>D</i> ... <i>A</i>	<i>D</i> —H... <i>A</i>
N2—H2C...C11 <sup>ii</sup>	0.89	2.70	3.253 (3)	121.
N2—H2C...C11 <sup>iii</sup>	0.89	2.53	3.252 (3)	139.
N2—H2B...C11 <sup>iv</sup>	0.89	2.41	3.253 (3)	159.
N2—H2A...C11 <sup>v</sup>	0.89	2.46	3.252 (3)	148.
O1—H1E...C11 <sup>vi</sup>	0.85	2.42	3.183 (3)	150.
O1—H1D...C11 <sup>vii</sup>	0.82	2.38	3.183 (3)	167.
N1—H1C...C11 <sup>viii</sup>	0.90	2.22	3.101 (3)	165.
N1—H1B...O1 <sup>ix</sup>	0.90	1.78	2.678 (6)	172.
N1—H1A...C11 <sup>x</sup>	0.90	2.23	3.101 (3)	163.

Symmetry codes: (ii)  $x+1, -y+3/2, z$ ; (iii)  $-x+2, y-1/2, -z+1$ ; (iv)  $x+1, y-1, z$ ; (v)  $-x+2, -y+1, -z+1$ ; (vi)  $-x+1, -y+1, -z+1$ ; (vii)  $-x+1, y-1/2, -z+1$ ; (viii)  $x+1, y-1, z-1$ ; (ix)  $x, y, z-1$ ; (x)  $x+1, -y+3/2, z-1$ .



Fig. 1

